

Cryptonote over Ring-LWE

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The equations below were a draft inspired by "Unlinkable payments" and "One-time ring signatures" in Cryptonote(<https://cryptonote.org/>) over Ring-LWE, which is one of Post-Quantum cryptography.

Does it make sense?

Or please let me know if there already exists similar or better idea in some papers etc.

1 Unlinkable Payments

Setup: Select $A \in R_q$

1. Bob makes a private key $s_A, s_B \in R_q$ and its public key $P_A = As_A + e_A, P_B = As_B + e_B, e_A, e_B \in \chi$.
2. Alice makes an ephemeral private key $r \in R_q$ and one time public key $P_{epm} = Ar + e_1, e_1 \in \chi$.
3. Alice does key exchange by NewHope(<https://eprint.iacr.org/2015/1092.pdf>) etc with Bob's public key P_A and get $K \in R_q$
4. Alice computes one time public key $P = AH_s(K) + P_B$.
5. Alice sets P and P_{epm} as a destination key in a transaction.
6. Bob does key exchange with P_{epm} and gets K .
7. Bob computes $P = AH_s(K) + P_B = A(H_s(K) + s_B) + e_B$ and its private key $H_s(K) + s_B$.

2 One-time ring signatures

Setup: Select $A \in R_q$

1. The signer picks a random secret key $x \in R_q$ and computes public key $P = Ax + e$ and the key image $I = H_p(P)x + e$.
2. He picks a random $\{q_i | i = 0 \dots n\}, \{w_i | i = 0 \dots n\}$ and $\{e_i | i = 0 \dots n\}$ and applies the following transformations:
$$L_s = Aq_s + e_s$$
$$L_i = Aq_i + e_i + w_i P_i \quad (i \neq s)$$
$$R_s = H_p(P)q_s + e_s$$
$$R_i = H_p(P_i)q_i + e_i + w_i I \quad (i \neq s)$$
3. He gets a non-interactive challenge: $c = H_s(m, L_1, \dots, L_n, R_1, \dots, R_n)$
4. He computes the response:
$$c_i = w_i \quad (i \neq s)$$
$$c_s = c - \sum_{i=0}^n c_i$$
$$r_i = q_i \quad (i \neq s)$$
$$r_s = q_s - c_s x \text{ mod } l$$
$$t_i = e_i \quad (i \neq s)$$
$$t_s = e_s - c_s e \text{ mod } l$$

The signature is $\sigma = (I, c_1 \dots c_n, r_1 \dots r_n, t_1 \dots t_n)$
5. The verifier checks the signature by:
$$L'_i = Ar_i + t_i + c_i P_i$$
$$R'_i = H_p(P_i)r_i + t_i + c_i I$$

and $\sum_{i=0}^n c_i = ? H_s(m, L'_1, \dots, L'_n, R'_1, \dots, R'_n)$